

SPECIFICATION

TO ALL WHOM IT MAY CONCERN:

BE IT KNOWN that we KUNIO KOBAYASHI, a subject of Japan and residing at Shinjuku-ku, Tokyo, Japan, HIKARU MORITA a subject of Japan and residing at Shinjuku-ku, Tokyo, Japan and KOUTAROU SUZUKI a subject of Japan and residing at Shinjuku-ku, Tokyo, Japan have invented certain new and useful improvements in

"SYSTEM AND METHOD FOR QUANTITATIVE COMPETITION AND RECORDING MEDIUM HAVING RECORDED THEREON PROGRAM FOR IMPLEMENTING THEM"

and we do hereby declare that the following is a full, clear and exact description of the same; reference being had to the accompanying drawings and the numerals of reference marked thereon, which form a part of this specification.

SYSTEM AND METHOD FOR QUANTITATIVE COMPETITION AND
RECORDING MEDIUM HAVING RECORDED THEREON PROGRAM
FOR IMPLEMENTING THEM

5 BACKGROUND OF THE INVENTION

The present invention relates to a quantitative competition system and method which compare aimed or intended values of participants and publish the highest or lowest value but hide the other values, and a recording medium on which there is recorded a program for implementing the method. More particularly, the invention pertains to a system and method for quantitative comparison of secret values, for example, in electronic lottery, electronic voting, or electronic sealed-bid auction under circumstances where many participants are allowed to access the server online across the Internet.

Fig. 1 is depicts in block form the configuration of a conventional electronic competitive bidding or sealed-bid auction system. A notice of auction is input to bidding devices 10_1 to 10_M , which send their identifiers ID_1 to ID_M and bidding prices PR_1 to PR_M to a bid-opening device 20. In this transfer of each data, if it is desirable to keep the data secret, the bidding price is sent in compressed form, and if it is necessary to identify the data, it is sent together with a digital signature of the bidder. The bid-opening device 20 detects the highest (or lowest) one of the bid values received from the bidding devices 10_1 to 10_M , and outputs the winning bid and the identifier corresponding thereto. This scheme is disclosed, for example, in Japanese Patent Application Laid-Open Gazette No. 118876/90 entitled "Electronic Bidding System." On the other hand, schemes which publish only the winning bid but hide other information involved are disclosed, for example, in Kazuo SAKO, "Auction Protocol Which Hides Bids of Losers," The

Symposium on Cryptography and Information Security, SCIS'99, and in Shingo MIYAZAKI and Kouichi SAKURAI, "A Bulletin-Board Base Digital Auction Scheme with Bidding Down Strategy," The Symposium on Cryptography and Information Security SCIS'99.

5 The sealed-bid auction scheme to which the present invention is applied satisfies the requirements mentioned below.

 *Only bidding prices are used to determine the winning bid; that is, the successful bidding device is not determined using other information.

 * The bid-opening device and a provisional identifier registration
10 device neither cheat nor malfunction.

SUMMARY OF THE INVENTION

 It is therefore an object of the present invention to provide a quantitative competition system and method which ensure the fairness of a
15 sealed-bid auction, the validity of a successful bid value, the undeniability of bidders, the anonymity of the bidders and the freedom from double bidding.

 The fairness of an auction means that it is possible to prevent bidders from obtaining information on other bidding devices prior to bidding in an attempt to make bids with unfair advantage.

20 The validity of a successful bid value means that it is possible to prevent an unfair determination of the winning bid.

 The undeniability of bidders means that it is possible to prevent them from denying their bid values at the bid-opening time.

 The anonymity of bidders means that it is possible to prevent leakage
25 of identification information of every bidding device.

 According to the present invention, each bidding device transforms its bidding price to bidding price information through utilization of a one-way

function, and the bid-opening device uses the bidding price information to determine the successful bid without revealing the prices bid by unsuccessful bidders.

5 BRIEF DESCRIPTION OF THE DRAWINGS

Fig. 1 is a block diagram showing the general configuration of an electronic competitive bidding system;

Fig. 2 is a flowchart showing the general procedure of an electronic sealed-bid auction;

10 Fig. 3 is a block diagram depicting a bidding device which uses one-way functions to generate a bid index;

Fig. 4 is a block diagram depicting a concrete example of a bidding price transformer using one-way function processors;

15 Fig. 5 is a flowchart showing the procedure for generating the bid index through the use of one-way functions;

Fig. 6 is a block diagram illustrating the functional configuration of a bid-opening device 20 in a first embodiment of the present invention which is designed to determine the highest price bid as the winning bid;

20 Fig. 7 is a flowchart showing the operation of the bid-opening device 20 depicted in Fig. 6;

Fig. 8 is a block diagram illustrating the functional configuration of a bid-opening device in a second embodiment of the present invention;

Fig. 9 is a flowchart showing the operation of the bid-opening device depicted in Fig. 8;

25 Fig. 10 is a block diagram illustrating the functional configuration of a bid-opening device in a third embodiment of the present invention which is designed to determine the highest price bid as the winning bid;

Fig. 11 is a flowchart showing the bid-opening procedure of the bid-opening device depicted in Fig. 10;

Fig. 12 is a block diagram illustrating the functional configuration of a bidding device in a fourth embodiment of the present invention;

5 Fig. 13 is a block diagram illustrating the functional configuration of a bid-opening device in the fourth embodiment;

Fig. 14 is a flowchart showing the bid-opening procedure of the bid-opening device depicted in Fig. 13;

10 Fig. 15 is a block diagram illustrating the functional configuration of a bidding device in a fifth embodiment of the present invention;

Fig. 16 is a flowchart showing the bidding procedure of the bidding device depicted in Fig. 15;

Fig. 17 is a block diagram illustrating the functional configuration of a bid-opening device in a fifth embodiment of the present invention;

15 Fig. 18 is a flowchart showing the bid-opening procedure of the bid-opening device depicted in Fig. 17;

Fig. 19 is a flowchart showing the bid-opening procedure in a modified form of the fifth embodiment;

20 Fig. 20 is a block diagram illustrating the functional configuration of a bidding device in a sixth embodiment of the present invention;

Fig. 21 is a flowchart showing the bidding procedure of the bidding device depicted in Fig. 20;

Fig. 22 is a block diagram illustrating the functional configuration of a bid-opening device in the sixth embodiment;

25 Fig. 23 is a flowchart showing the bid-opening procedure of the bid-opening device depicted in Fig. 22;

Fig. 24 is a flowchart showing a modified form of the bid-opening

procedure depicted in Fig. 23;

Fig. 25 is a block diagram illustrating the functional configuration of a bidding device in a seventh embodiment of the present invention;

Fig. 26 is a flowchart showing the bidding procedure of the bidding device depicted in Fig. 25;

Fig. 27 is a block diagram illustrating the functional configuration of a bid-opening device in the seventh embodiment;

Fig. 28 is a flowchart showing the bid-opening procedure of the bid-opening device depicted in Fig. 27;

Fig. 29 is a flowchart showing a modified form of the bid-opening procedure depicted in Fig. 28;

Fig. 30 is a block diagram illustrating the functional configuration of a bidding device in an eighth embodiment of the present invention;

Fig. 31 is a block diagram illustrating the functional configuration of a bid-opening device in the eighth embodiment;

Fig. 32 is a flowchart showing the bid-opening procedure of the bid-opening device depicted in Fig. 31;

Fig. 33 is a block diagram illustrating an electronic sealed-bid auction system which utilizes a provisional identifier; and

Fig. 34 is a flowchart showing the bidding procedure in the system depicted in Fig. 33.

DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENTS

First Embodiment

The electronic competitive sealed-bid auction system according to this embodiment comprises, as is the case with Fig. 1, M bidding devices 10_1 to 10_M and a bid-opening device 21, which are accessible to each other. This

system operates as depicted in the flowchart of Fig. 2.

Step S1: Input a notice of auction to each of the bidding devices 10_1 to 10_M . The notice of auction describes bidding conditions such as the name of an object for auction, the highest and/or lowest price bid, the term for bidding and qualifications for bidding, and a method of access to the bid-opening device. The bidding conditions differ with objects for auction.

Step S2: In response to the notice of auction which describes the details of the auction, each bidding device 10_m (where $m = 1, 2, \dots, M$) generates a bidding price, and sends to the bid-opening device 20 the bidding price PR_m and an identifier ID_m by which the bidding device 10_m can be identified.

Step S3: Having received from the respective bidding device 10_1 to 10_M their bidding prices PR_1 to PR_M and identifiers ID_1 to ID_M , the bid-opening device 20 computes the highest (or lowest) one of the bidding prices and determines it to be the winning bid.

Step S4: The bid-opening device 20 outputs the winning bid and the identifier of the bidding device having submitted it.

The above procedure is the same as in the prior art. Since the communication channel between each bidding device 10_m and the bid-opening device 20 is not an anonymous channel, in particular, such a procedure as shown in Fig. 2 allows each bidding device 10_m to learn the bidding prices of the other bidding devices by wiretapping. To avoid this, according to the present invention, each bidding device 10_m uses one-way functions to transform the bidding price to bidding price information, which is sent to the bid-opening device 20.

Referring to Fig. 3, the bidding device 10_m comprises an input part 11, an information storage part 12, a control part 13 and a bidding price

transformer 14. The control part 13 follows a control procedure stored in the information storage part 12 to control operations of the respective parts. The notice of auction, which describes the bidding conditions, is provided in advance via a channel to the bidding device 10_m from the bid-opening device 20 or some other device. In the information storage part 12 there are also stored the identifier ID_m of this bidding device 10_m and an initial value IV_m which is used for bidding. At the time of bidding, the bidding price PR_m provided to the input part 11 is fed via the control part 13 into the bidding price transformer 14. The bidding price transformer 14 uses one-way functions to transform the bidding price PR_m to bidding price information γ_m in integral form. The bidding price information γ_m and the identifier ID_m are sent from a transceiver (not shown) to the bid-opening device 20 via a communication channel. Based on the bidding price information from every bidding device 10_m , the bid-opening device 20 decides the winning bid.

In this embodiment, the bidding price transformer 14 is supplied with the initial value IV_m read out of the information storage part 12 by the control part 13 and the bidding price PR_m , and processes the initial value IV_m by a one-way function by the number of times corresponding to the bidding price PR_m as described below. A one-way function is such a function that, given a variable x , $y(=h(x))$ can easily be computed from x , but when given y , very high computational complexity is needed to compute x such that $y=h(x)$. An output value, obtained by processing the initial value IV_m with the one-way function h by k times like $h(\dots h(h(h(IV_m))))\dots$, will hereinafter be represented by $h^k(IV_m)$.

A concrete example of the bidding price transformer 14 is depicted in Fig. 4 and its procedure in Fig. 5. The bidding price transformer 14 comprises a data storage part 14S, conversion table memory 15, a one-way

function h processor 16 and a one-way function g processor 17. Incidentally, the examples of the bidding device 10_m depicted in Figs. 3 and 4 will also be referred to in describing second and third embodiments of the invention later on, in which case the broken-lined data storage part 14S is provided to store the result D_m of each computation by the one-way function h and the final result C_m of computation. A conversion table, which is stored in the conversion table memory 15, is contained as one bidding condition in the notice of auction, for instance. Each bidding device 10_m reads out the conversion table from a bulletin board 25 of the bid-opening device 20 which will be described later on with reference to Fig. 6. The conversion table is a table on which there are shown appropriately-separated K bidding prices from the lowest to the highest bidding price and a series of corresponding indexes $k = 1, 2, \dots, K$. Each bidding device 10_m selects a desired bidding price from the conversion table and uses the corresponding index k as a bidding price index k_m . In the Fig. 4 example the bidding prices corresponding to the indexes $k = 1, 2, \dots, K$ are arranged to monotonously increase, but by arranging them to monotonously decrease, the lowest bidding price can be made a winning bid.

The one-function h processor is supplied with the initial value IV_m and the price index k_m corresponding to the bidding price PR_m read out of the conversion table memory 15, and repeatedly processes the initial value IV_m with the one-way function h by the number of times corresponding to the price index k_m . As a result, $h^{k_m}(IV_m)$ is obtained. The one-way function g processor 17 further processes the output value $h^{k_m}(IV_m)$ with a one-way function g to compute $\gamma_m = g(h^{k_m}(IV_m))$, and output it as bidding price information.

Step S1: Input the bidding price PR_m and the initial value IV_m .

Step S2: Read out of the conversion table memory 15 the price index k_m corresponding to the bidding price PR_m .

Step S3: In the one-way function h processor 16, set the initial value of a variable t at 0 and the initial value IV_m as γ_m , and repeat steps S4 and S5.

5 Step S4: Determine if t is smaller than k_m .

Step S5: If $t < k_m$, update γ_m with the value of $h(\gamma_m)$ at that time, then increment t by one, and return to step S4.

10 Step S6: When t becomes no longer smaller than k_m , $\gamma_m = h^{k_m}(IV_m)$, which is processed by the one-way function g processor 17 such that $\gamma_m \leftarrow g(\gamma_m)$.

Step S7: Output, as the bidding price information, γ_m obtained in step S6.

BID-Opening Device (Successful Bid: Highest Bidding Price Bid)

15 Fig. 6 is a block diagram of the bid-opening device 20, which comprises a control unit 21, and a one-way function h processor 22, a one-way function g processor 23, an adder/subtractor 24, a bulletin board 25, a program storage part 27S, an information storage part 35 and an update data storage part 36 which are all connected to the control unit 21. In the program storage part 27S there is stored a bid-opening procedure as a
20 program, and the control unit 21 follows the program to control operations of the respective parts. The one-way function h processor 22 and the one-way function g processor 23 are series-connected. The parts except the bulletin board 25 constitute a winning bid selector 27. The number of bidding devices are M , and the initial value IV_m unique to each bidding device 10 _{m} (where $m = 1, 2, \dots, M$) is prestored by some means in the information
25 storage part 35. In the bulletin board 25 there are also recorded other bidding conditions including a conversion table 25A; furthermore,

verification information and the results of auction to be published are written in the bulletin board 25. The pieces of information are accessible from any external devices as well as from the bidding devices. In this case, however, assume that only the bid-opening device 20 is allowed to write in the bulletin board 25 (This applies to other embodiments).

In Fig. 7 there is depicted the procedure of operation of the bid-opening device 20. In this example the bidding price corresponding to the largest price index k_m is made a successful bid as follows. The index value is decremented one by one from the largest index K corresponding to the upper limit of the bidding price specified in the conversion table; a check is made for the presence of the bidding price information γ_m (where $m = 1, 2, \dots, M$) corresponding to each index k is present; and when the bidding price information γ_m corresponding to the index k is detected for the first time, the detected bidding price information γ_m is determined to be the winning bid, and m (the bidding device number) at that time is computed, with which the bid-opening procedure ends.

Step S0: The bidding device 10_m inputs its bidding price information γ_m and identifier ID_m (where $m = 1, 2, \dots, M$) to the bid-opening device 20.

Step S1: The control unit 21 records the bidding price information γ_m and the identifier ID_m in the bulletin board 25 accessible from arbitrary external devices (the bidding devices 10_1 to 10_M and other devices which are not bidders).

Step S2: To precalculate $D_m^{(1)}, D_m^{(2)}, \dots, D_m^{(K)}$ such that $D_m^{(k)} = h(D_m^{(k-1)})$ in the subsequent steps S3 to S6, the control unit 21 sets the bidding price index $k \leftarrow 1$, then reads out ID_m from the information storage part 35, and substitutes it for $D_m^{(0)}$.

Step S3: The control unit 21 determines whether $k > K$.

Step S4: If not $k > K$, process $D_m^{(k-1)}$ by the one-way function h processor 22 to obtain $D_m^{(k)}$.

Step S5: Store $D_m^{(k)}$ in the update data storage part 36.

Step S6: Increment k by the adder/subtractor 24 such that $k \leftarrow k+1$.

5 Step S7: If $k > K$ in step S3, it means that $D_m^{(1)}=h(D_m^{(0)})=h(IV_m)$, $D_m^{(2)}=h(D_m^{(1)})=h^2(IV_m)$..., $D_m^{(K)}=h^K(IV_m)$ have all been obtained, then set $k \leftarrow K$.

10 Step S8: Read out $D_m^{(K)}=h^K(IV_m)$ from the update data storage part 36 and process it by the one-way function g processor 23 to obtain $D_m^{(k)} \leftarrow g(D_m^{(K)})$.

Step S9: For $m = 1, 2, \dots, M$, the control unit 21 makes a check to see if there exists on the bulletin board 25 the bidding price information γ_m of the same value as $D_m^{(k)}$.

15 Step S10: If there does not exist on the bulletin board 25 the information γ_m of the same value as $D_m^{(k)}$, the control unit 21 inputs k to the adder/subtractor 24 to decrement k by one (i.e., $k \leftarrow k-1$), then returns to step S8, and in steps S8 and S9 it makes a check to see if there exists on the bulletin board 25 the bidding price information γ_m of the same value as $D_m^{(k)}=g(h^k(IV_m))$ for $m = 1, 2, \dots, M$.

20 Step S11: If the information γ_m of the same value as $D_m^{(k)}$ is found on the bulletin board 25 in step S9, then the control unit 21 regards it as the successful price bid and outputs the index k at this time and the bidding device identifier ID_m corresponding to the information γ_m , with which the procedure ends.

25 As described above, a check is made first for a bidding device 10_m having input the bidding price information γ_m equal to $D_m^{(k)} (=g(h^k(IV_m)))$ when the price index k is at the upper limit value K ; if no such a bidding

device is found, then a check is made for a bidding device 10_m having input the bidding price information γ_m equal to $D_m^{(k)}$ when the index k is decremented by one, i.e. $k \leftarrow k-1$; and if no such a bidding device is found, then a check is made for a bidding device 10_m having input the bidding price information γ_m equal to $D_m^{(k)}$ when the index is further decremented by one, i.e. $k \leftarrow k-1$. By making a check, for each decremented value of k , for the bidding device 10_m having input the bidding price information γ_m equal to $D_m^{(k)} (=g(h^k(IV_m)))$, it is possible to find out the price information γ_m corresponding to the largest index k , that is, the highest bidding price PR_m .

Furthermore, each bidding device 10_m sends $h^{k_m+1}(IV_m)$ to the bid-opening device 20 in advance, and the bid-opening device 20 publishes it on the bulletin board 25 and, after determining the successful bidding price, publishes on the bulletin board 25 the highest bidding price index k and the identifier ID_m of the successful bidding device and the verification information $h^k(IV_m)$; in this instance, since k ought to equal k_m , it is possible for an arbitrary device, except the bid-opening device 20, to verify the validity or fairness of the bid-opening process by processing the published verification information $h^k(IV_m)$ with the one-way function h to obtain $h^{k+1}(IV_m)$ and making sure that it matches $h^{k_m+1}(IV_m)$ published prior to the determination of the winning bid. Alternatively, the verification of the bid-opening procedure can be made by publishing the verification information $h^k(IV_m)$ of each bidding device on the bulletin board 25 in advance and making a check to see if the value, obtained by processing $h^{k_m}(IV_m)$ published on the bulletin board 25 with the one-way function h by $(K-k_m)$ times, matches $h^k(IV_m)$.

In the case where the lowest price bid is the winning bid, the bidding prices corresponding to the price indexes k on the conversion table are arranged so that they monotonously increase from the lowest value, as

referred to previously.

In the embodiment described above, all the bidding device 10_1 to 10_M send $h^{k_m+1}(IV_m)$ to the bid-opening device 20 in advance for verification of the results of bid-opening, and the bid-opening device 20 writes it on the bulletin board. It is easy to compute $h^{k+1}(z)$ from $h^k(z)$ in the computation $h^{k+1}(z)=h(h^k(z))$ using the one-way function, but the computation of $h^k(z)$ from $h^{k+1}(z)$ involves too enormous computational complexity to deal with practically. Accordingly, even if the bidding device publishes in advance $h^{k_v}(IV_m)$ computed using an index k_v larger than the bidding price index k_m , there is no possibility of other devices learning the index k_m unless the bid-opening is performed in terms of the index k_m .

The value k_v of the verification information $h^{k_v}(IV_m)$ may be a value $k_v=k_m+A$ which is obtained by adding the bidding price index k_m with a predetermined integer A equal to or greater than 1, or a value $k_v=K+A$ which is obtained by adding the maximum index K with the integer A . In the former case, $h^{k_m}(IV_m)$ is processed A times with the one-way function h and the resulting value is checked for matching the published information $h^{k_v}(IV_m)$. In the latter case, $h^{k_m}(IV_m)$ is processed $K+A-k_m$ times with the one-way function h and the resulting value is checked for matching the published information $h^{k_v}(IV_m)$.

In the embodiment described above, the bidding devices 10_1 to 10_M each convert the bidding price PR to the index k by the conversion table and the initial value IV_m is processed with the one-way function by the number of times corresponding to the index k , but the use of the conversion table is not essential to the present invention. For example, the index k itself may be the bidding price, in which case neither of the bidding devices the bid-opening device requires the conversion table and any one of a series of value k which

monotonously increase one by one within a predetermined range defined by the upper and lower limits given as one of the conditions for auction is chosen as the bidding price PR.

5 SECOND EMBODIMENT

In the first embodiment the bid-opening device 20 must be informed of the initial value IV_m of each bidding device 10_m . In this embodiment, however, the bid-opening device 20 requires the bidding device 10_m to send $D_m = h^k(IV_m)$ corresponding to the price index k , and hence it does not need the
 10 initial value IV_m . Since the price index k varies one by one such that $k = 1, 2, \dots, K$, this embodiment utilizes the fact that $h^{k+1}(IV_m) = h(h^k(IV_m))$ holds; the bid-opening device 20 verifies the response $h^k(IV_m)$ from the bidding device in reply to an inquiry k , then computes $g(h^k(IV_m))$, and checks it for matching the bidding price information γ_m (where $m = 1, 2, \dots, M$).

15 A description will be given of the case where the highest bid is the successful bid.

The bidding device 10_m has a configuration in which the data storage part 14S indicated by the broken line in Fig. 4 is added to the bidding price transformer 14. The bidding device 10_m precomputes $D_m = h^k(IV_m)$ by the
 20 one-way function h processor 16 for each value $k = 1, 2, \dots, K+1$, and stores it in the data storage part 14S. When inquired about k from the bid-opening device 20, the bidding device 10_m reads out of the data storage part 14S the data $h^k(IV_m)$ corresponding to k and sends it as the response $D_m = h^k(IV_m)$ to the bid-opening device 20. Furthermore, the bidding device 10_m sends to the
 25 bid-opening device 20 the data $h^{K+1}(IV_m)$ as the verification information C_m , together with the bidding price information γ_m . As depicted in Fig. 8, the bid-opening device 20 comprises a control unit 21, a one-way function h

processor 22, a one-way function g processor 23, a subtractor 24, a program storage part 27S and a bulletin board 25 accessible from other devices. On the bulletin board 25 there are published a conversion table 25A along with conditions for auction.

5 The bid-opening device 20 operates as depicted in Fig. 9.

 The bidding devices 10_m each send $h^{K+1}(IV_m)$ as the verification information C_m in advance to the bid-opening device 20 together with the bidding price information γ_m and the identifier ID_m . The bid-opening device 20 publishes these pieces of data on the bulletin board 25. Let it be assumed
10 here that M bids are submitted, and hence $m = 1, 2, \dots, M$.

 Step S1: Write and hence publish on the bulletin board 25 the plural pieces of data sent to the bid-opening device 20, that is, the bidding price information $\gamma_m (=g(h^{km}(IV_m)))$, the verification information C_m and the identifier ID_m .

15 Step S2: Set the initial value of the index k at the upper limit value K by control unit 21.

 Step S3: Request each bidding device 10_m to present $D_m = h^k(IV_m)$. The bidding device 10_m reads out of the data storage part 14S the data $h^k(IV_m)$, and sends it to the bid-opening device 20 as D_m .

20 Step S4: Record and hence publish on the bulletin board 25 the data D_m sent from every bidding device 10_m .

 Step S5: Generates $h(D_m)$ for each D_m by the one-way function h processor 22.

 Step S6: Make a check to see if all the pieces of data $h(D_m)$ match all
25 the pieces of verification information C_m on the bulletin board 25; if no mismatch is found, then determine that they are all correct or valid, and continue the subsequent steps. If a mismatch is found, then sends an error

message to every bidding device 10_m and finish the bid-opening operation.

Step S7: When no mismatch is found in step S6, generate data $g(D_m)$ by the one-way function g processor 23.

Step S8: Make a check to see if each data $g(D_m)$ matches the bidding price information γ_m ; if no match is found, update C_m on the bulletin board 25 with D_m ($C_m \leftarrow D_m$).

Step S10: Set $k \leftarrow k-1$ by the subtractor 24 and return to step S3.

Step S11: If even one of the pieces of information γ_m is found to match with $g(D_m)$ in step S8, decide k at that time as the price index corresponding to the winning bid, and output the index k and the identifier ID_m of the bidding device 10_m having offered the successful bid.

In this instance, the values of losing bids other than the winning one are kept secret from even the bid-opening device 20.

In this embodiment, too, the lowest price bid can be chosen as the winning bid simply by arranging the bidding prices in such a manner as to monotonously decrease relative to a monotonously increasing index k on the conversion table, or by arranging the bidding prices in such a manner as to monotonously increase relative to a monotonously decreasing index k .

20 THIRD EMBODIMENT

In the second embodiment described above, as depicted in Fig. 9, the bid-opening device 20 requires all the bidding devices to present $h^k(IV_m)$ and receive it for each value of the price index k until the first detection of a match between $g(D_m)$ and γ_m in step S3. Accordingly, the sealed-bit auction scheme according to the second embodiment has the defect of a large communication cost. This embodiment requires the bid-opening device 20 to be informed of nothing but the initial value IV_m , publishes only the winning

bid, that is, hides the losing bids, and reduces the communication cost.

The bidding device 10_m is identical in construction as in the second embodiment, and in the constructions of figs. 3 and 4 the data storage part 14S is provided in which there are prestored $D_m^{(1)}, \dots, D_m^{(K)}$ and $C_m = D_m^{(k+1)}$.

5 The bid-opening device 20, shown in Fig. 10, is basically identical in construction with the bid-opening device of Fig. 8, and no description will be repeated, but as will be described below with reference to Fig. 11, the operation of the bid-opening device in this embodiment differs from the operation depicted in Fig. 9.

10 Step S0: The bidding devices 10_1 to 10_M each send in advance the verification information $C_m (= h^{k+1}(IV_m))$ to the bid-opening device 20 together with the bidding price information $\gamma_m (= g(h^{km}(IV_m)))$ and the identifiers ID_m .

15 Step S1: The bid-opening device 20 first publishes the plural pieces of bidding price information γ_m and verification information C_m and the identifiers ID_m on the bulletin board 25.

Step S2: Set the count value k of a counter 24 at the upper limit value K .

20 Step S3: Inquire of all the bidding devices 10_m (where $m = 1, 2, \dots, M$) about whether they have bid the price k .

Step S4: Decide whether there is bidding device having bid with the price index k .

Step S5: If no bidding device have bid the price, decrement k by the subtractor 24 to $k \leftarrow k-1$ and return to step S3.

25 Step S6: When it is found that any one of the bidding devices 10_m has bid with the price index k , request all the bidding devices 10_m to present $h^k(IV_m)$. Each bidding device 10_m reads out of the data storage part 14S the

data $D_m = h^k(IV_m)$ precalculated corresponding to k as depicted in Fig. 4, and sends the read-out data D_m to the bid-opening device 20.

Step S7: Publishes all the responses D_m from the bidding devices 10_m on the bulletin board 25.

5 Step S8: For all the responses D_m , generate $h^{K-k+1}(D_m)$ by the one-way function h processor 22.

Step S9: Check whether each data $h^{K-k+1}(D_m)$ matches the corresponding verification information C_m on the bulletin board 25. If no mismatch is found, decide that the responses D_m are all correct, and proceed
10 to the subsequent steps. If a mismatch is found, send an error message to each bidding device 10_m and finish this bid-opening session for the price index k .

Step S10: When no mismatch is found in step S9, generate $g(D_j)$ by the one-way function g processor 23 for the response D_j (where $1 \leq j \leq M$) from
15 the bidding device 10_j which has identified itself as having bid with the price k .

Step S11: Check whether $g(D_j)$ matches the bidding price information γ_j of the bidding device 10_j on the bulletin board 25. If they match, decide that the bidding device 10_j has bid the price k . If they do not match, send an
20 error message to all the bidding devices and discontinue the session.

As described above, in this embodiment, when no bidding device identifies itself as having bid the price k in reply to the inquiry in step S3, the bidding devices 10_m are not required to send $D_m (= h^k(IV_m))$ to the bid-opening device 20, and hence the communication cost is small as compared
25 with that in the second embodiment accordingly.

As described below, a check is made, if necessary, to see if another bidding device 10_m (different from the device 10_j) has bid a value higher than

k.

Step S12: For t such that $k \leq t \leq K$ and all m 's except j ($1 \leq m \leq M$, $m \neq j$), it is checked whether $g(h^{t-k}(h^k(IV_m)))$ matches the bidding price information γ_m on the bulletin board 25 for $t = k, k+1, \dots, K$, and if a match is found, then
 5 send an error message to each bidding device concerned and discontinue the bid-opening session.

Step S13: If no match is found, then output the winning bidding price k and the identifier ID_j of the bidding device having offered the winning bid.

With this check or verification, if a bidding device makes a false
 10 response to the inquiry about whether it has bid, for example, with k , this dishonest bidding device is detected; that is, this embodiment satisfies the "undeniability" requirement. When this checking does not take place, the bid-opening device 20 outputs k and ID_j when deciding in step S11 that the bidding device 10_j has bid with k .

15 In this way, this embodiment keeps losing bids, except the winning one, secret from even the bid-opening device 20 and reduces the communication cost.

While in the above the highest price bid is the winning bid, the lowest price bid can be chosen as the successful bid simply by arranging
 20 monotonously decreasing (or increasing) values of the bidding price PR on the conversion table in a one-to-one correspondence with monotonously increasing (or decreasing) values of the price index k .

FOURTH EMBODIMENT

25 This embodiment is intended to permit simplification of the processing in the bid-opening device 20 and reduction of the communication cost.

As depicted in Fig. 12, each bidding device 10_m has a construction in which a random generator 18 and an operation part 19 are added to the bidding device shown in Figs. 3 and 4. The random generator 18 generates a random number R_m known only to the bidding device 10_m . The operation part 19 uses the random number R_m and the bidding price PR_m to perform a predetermined operation such as a bit concatenation, exclusive ORing, addition, or multiplication (which operation will hereinafter be denoted by (+)), then processes the operation result with the one-way function h , and sends the processed output $h(PR_m(+) R_m)$ to the bid-opening device 20, together with the bidding price information $\gamma_m = g(h^{km}(IV_m))$ and the identifier ID_m .

Fig. 13 illustrates in block form the functional configuration of the bid-opening device 20 in this embodiment, and Fig. 14 is a flowchart for explaining its operation. The bid-opening device 20 has a construction in which one-way function h processors 22' and 22'' and an operation part 26 are added to the device of Fig. 10 and a subtractor 37 is replaced for the counter 24. For simplicity sake, the program storage part 27S is not shown. At the time of bidding every bidding device 10_m (where $m = 1, 2, \dots, M$) sends $h^{K+1}(IV_m)$ to the bid-opening device 20, along with the bidding price information $\gamma_m (= g(h^{km}(IV_m)))$, the identifier ID_m and the random number information $h(PR_m(+) R_m)$.

Step S1: Receive γ_m , $C_m (= h^{K+1}(IV_m))$, $h(PR_m(+) R_m)$ and ID_m from each bidding device 20 and write and hence publish them on the bulletin board 25.

Step S2: Request all the bidding devices 10_m to present their bidding prices PR_m and random numbers R_m .

Step S3: Upon receiving PR_m and R_m from each bidding device 10_m , compute $(PR_m(+)R_m)$ in the operation part 26, then compute $h(PR_m(+)R_m)$ by

the one-way function h processor 22'', and make a check to determine whether the value matches $h(PR_m(+)R_m)$ published on the bulletin board 25.

Step S4: At this point the bid-opening device 20 learns all the bidding prices. The bid-opening device 20 obtains from the conversion table 25A a price index k_{mx} corresponding to the highest value among the bidding prices PR_m . The bidding device (the successful bidding device) which has bid k_{mx} will hereinafter be identified by 10_j . At this point each bidding device cannot learn the bidding prices of the other bidding devices.

Step S5: Send k_{mx} to all the bidding devices 10_m and request them to present $D_m = h^{k_{mx}}(IV_m)$.

Step S6: Each bidding device 10_m reads out $D_m = h^{k_{mx}}(IV_m)$ corresponding to k_{mx} from the data storage part 14S described previously with respect to Fig. 4, and sends the read-out D_m to the bid-opening device 20, which writes on the bulletin board 25 all the pieces of data D_m sent from the bidding devices 10_m .

Step S7: For each D_m , calculates $K+1-k_{mx}$ by a subtractor 37 and generate $h^{K+1-k_{mx}}(D_m)$ by the one-way function h processor 22 from $K+1-k_{mx}$ and D_m .

Step S8: Verify whether $h^{K+1-k_{mx}}(D_m)$ matches the corresponding verification information C_m on the bulletin board 25. If no mismatch is found, decides that all the responses D_m are correct, and proceed to the subsequent steps. If a mismatch is found, sends an error message to each bidding device and discontinue further operation.

Step S9: If no mismatch is found in step S8, generate $g(D_j)$ by the one-way function g processor 23 for D_j presented by the successful bidding device 10_j .

Step S10: Verify whether $g(D_j)$ matches the bidding price information

γ_j in the bidding data of the bidding device 20_j on the bulletin board 25. If they match, decide that the bidding device 10_j has bid with the price index k_{mx} . If they do not match, send an error message to each bidding device and discontinue the current bid-opening session.

- 5 As described below, a check is made, if necessary, to see if another bidding device 10_m (different from the device 10_j) has bid a value higher than k_{mx} .

Step S11: For $t = k_{mx} + 1, k_{mx} + 2, \dots, K$, compute $h^{t-k_{mx}}(D_m)$ by the one-way function processor 22' and process the computed result by the one-way function g processor 23 to obtain $g(h^{t-k_{mx}}(D_m))$, and verify whether this $g(h^{t-k_{mx}}(D_m))$ matches the bidding price information γ_m on the bulletin board 25 for all m 's except j ($1 \leq m \leq M, m \neq j$).

- Step S12: If a match is found, then send an error message to each bidding device concerned and discontinue the current bid-opening session.
- 15 If no match found, then output the winning bidding price index k_{mx} and the identifier ID_j of the bidding device 10_j having offered the winning bid.

For example, in the case where the bidding device 10_m bids with the random number information $h(PR_m(+)R_m)$ and the bidding price information $\gamma_m = g(h^{k_{mx}}(IV_m))$ (where $PR_m' > PR_m$) and presents a price PR_m' higher than the bidding price PR_m and the random number R_m in reply to the request for the presentation of PR_m and R_m in step S2 and the price PR_m' becomes the highest bid value, if the bidding device presents $D_m = h^{k_{mx}}(IV_m)$ in reply to the request for the presentation of $h^{k_{mx}}(IV_m)$ in step S5, it will pass the verifications in steps S7 and S8, incurring the possibility that the price PR_m lower than PR_m' becomes the winning bid. However, this can be prevented because a mismatch is found between $g(D_m) = g(h^{k_{mx}}(IV_m))$ and $\gamma_m = g(h^{k_{mx}}(IV_m))$ in steps S10 and S11.

20

25

With the bid-opening device 20, it is possible to specify the winning bid and the corresponding successful bidding device from PR_m , R_m and ID_m with ease, reduce the communication cost and verify that the winning bidding price and the winning device determined from PR_m , R_m and ID_m are true.

5

FIFTH EMBODIMENT

In this embodiment each bidding device sends to the bid-opening device bidding price information containing select information which indicates whether to bid for each of K kinds of biddable prices. As depicted in Fig. 15, the bidding price transformer 14 of the bidding device 10m comprises a control part 41, a random generator 42, a one-way function h processor 43, a select information generator 45, a (+) operation part 46 and an adder 47.

Let PR_m represent that one of the K kinds of price indexes 1, 2, ..., K which the bidding device 10_m is to actually to bid. The select information denoted by $b_m^{(k)}$ is defined as follows: $b_m^{(k)} = 0$ when the bidding device 10^m does not bid for the price index k such that $1 \leq k \leq K$, and $b_m^{(k)} = 1$ when the bidding device 10_m bids for the price index k . Accordingly, only one piece of information $b_m^{(k)}$ exists for k such that $1 \leq k \leq K$. As mentioned above, the two values of the information $b_m^{(k)}$ may be any values as long as they differ from each other. The information $b_m^{(k)}$ is known only to the bidding device 10_m, which uses it as a random number for each value of the price index k . The bidding device 10_m outputs $\{ID_m, h(1(+)b_m^{(1)}(+)R_m^{(1)}), h(2(+)b_m^{(2)}(+)R_m^{(2)}), \dots, h(K(+)b_m^{(K)}(+)R_m^{(K)})\}$ as bidding price information.

A description will be given, with reference to Fig. 16, of the procedure by which K pieces of bidding price information are prepared.

Step S1: The bidding price PR_m is determined and input.

Step S2: Set the initial value of the price index k to 1.

Step S3: Make a check to see if $k \leq K$.

Step S4: If $k \leq K$, generate the random number $R_m^{(k)}$ by the random generator 42.

5 Step S5: Generate the rice select information $b_m^{(k)}$ by the select information generator 45 in accordance with the bidding price PR_m .

Step S6: The (+) operation part 46 inputs thereinto these pieces of information $R_m^{(k)}$ and $b_m^{(k)}$, and compute $k(+b_m^{(k)}(+R_m^{(k)}))$. (+) indicates a predetermined appropriate operation, which may be a concatenation, addition, subtraction, multiplication, or the like.

10

Step S7: Process the result of this operation by the one-way function h processor 43 to generate $h(k(+b_m^{(k)}(+R_m^{(k)}))$.

Step S8: Increment k by one by the adder 47, followed by a return to step S3.

15 Step S9: When k exceeds K and the processing for all values of k ends, the bidding device 10_m sends the identifier ID_m and the bidding price information $\{h(1(+b_m^{(1)}(+R_m^{(1)})), \dots, h(K(+b_m^{(K)}(+R_m^{(K)}))\}$ to the bid-opening device 20.

By generating the bidding price information for each price through utilization of the one-way function and sending all the pieces of bidding price information to the bid-opening device 20 as described above, the aimed bidding price can be kept secret.

20

Fig. 17 illustrates in block form the bid-opening device 20 which performs the bid-opening process based on such bidding price information sent thereto. The bid-opening device 20 comprises a control part 21, a one-way function h processor 22, a subtractor 24, an information storage part 35, a bulletin board 25 and a (+) operation part 51. As is the case with Fig. 8, the

25

program storage part 27S is also provided but is not shown for the sake of brevity.

Fig. 18 is a flowchart for explaining the operation of this bid-opening device 20.

5 Step S0: Receive the bidding price information $\{ID_m, h(1(+))b_m^{(1)}(+))R_m^{(1)}, h(2(+))b_m^{(2)}(+))R_m^{(2)}, \dots, h(K(+))b_m^{(K)}(+))R_m^{(K)}\}$ from the bidding device 10_m (where $m = 1, 2, \dots, M$).

Step S1: Write and hence publish the bidding price information on the bulletin board 25.

10 Step S2: Set the price index k to its highest value K .

Step S3: Request each bidding device 10_m to present the random number $R_m^{(k)}$.

15 Step S4: The bidding devices 10_m each send the random number $R_m^{(k)}$ to the bid-opening device 20, which writes all the random numbers $R_m^{(k)}$ on the bulletin board 25.

Step S5: Set $b_m^{(k)} = 1$, then input $b_m^{(k)}$ and $R_m^{(k)}$ to the (+) operation part 51 to perform an operation $k(+))1(+))R_m^{(k)}$, and process the result of operation by the one-way function h processor 22 to obtain $h(k(+))1(+))R_m^{(k)}$.

20 Step S6: For each m , make a check to see if a match is found between the calculated $h(k(+))1(+))R_m^{(k)}$ and $h(k(+))1(+))R_m^{(k)}$ on the bulletin board 25.

Step S7: If no match is found, decrement k such that $k \leftarrow k-1$, and return to step S3.

25 Step S8: If a match is found, determine the k as the successful price index k , then output the price index k and the identifier ID_m of the bidding device 10_m concerned, and discontinue the current bid-opening session.

As described above, according to this embodiment, the bidding price information corresponding to each price index is generated using the one-way

function and all the pieces of bidding price information are sequentially opened in decreasing order from the highest value. This enables non-winning bids to be kept secret.

In the case of choosing the lowest price bid as the successful bid in this embodiment, the bidding device 10_m similarly sends the bidding price information $\{ID_m, h(1(+)b_m^{(1)}(+)R_m^{(1)}), h(2(+)b_m^{(2)}(+)R_m^{(2)}), \dots, h(K(+)b_m^{(K)}(+)R_m^{(K)})\}$ to the bid-opening device 20. The bid-opening device 20 carries out about the same processing as depicted in Fig. 18, but in step S2 the lowest value 1 of the K kinds of biddable price indexes is set to k and in sep S6 the index k is incremented by one such that $k \leftarrow k+1$.

In the case of choosing the highest price bid as the winning bid in this embodiment, since random numbers $R_m^{(t)}$ received from all the bidding devices for t (where $k \leq t \leq K$) are recorded on the bulletin board 25 in step S4, it is possible to detect that $b_m^{(k)} = 0$ for the index larger than the winning price index k, by calculating $h(t(+)b_m^{(t)}(+)R_m^{(t)})$ and comparing it with $h(k(+)b_m^{(k)}(+)R_m^{(k)})$ published on the bulletin board 25. Accordingly, any one can determine if the winning price index k is correct.

In this embodiment it is also possible for each bidding device 10_m to send the set of random numbers $\{R_m^{(k)}\} (k=1, \dots, K)$ to the bid-opening device 20 in advance together with ID_m and $h(k(+)b_m^{(k)}(+)R_m^{(k)})$. In this case, however, the random number $R_m^{(k)}$ is not written on the bulletin board 25 but is stored in the broken-lined information storage part 35. In Fig. 19 there is shown a flowchart for explaining the processing which the bid-opening device 20 performs in such an instance.

Sep S0: Receive the bidding price information $\{ID_m, h(1(+)b_m^{(1)}(+)R_m^{(1)}), h(2(+)b_m^{(2)}(+)R_m^{(2)}), \dots, h(K(+)b_m^{(K)}(+)R_m^{(K)})\}$ and random number information $\{R_m^{(1)}, R_m^{(2)}, \dots, R_m^{(K)}\}$ from the bidding devices

10_m (where $m = 1, 2, \dots, M$).

Step S1: Write and hence publish only the bidding price information on the bulletin board 25 and store the random number information in the storage part 35 indicated by the broken line.

5 Step S2: Set the highest possible value K for the price index k .

Step S3: For all m 's, generate $h(k(+))1(+))R_m^{(k)}$ read out of the storage part 35 with $b_b^{(k)}=1$.

Step S4: Verify whether a match is found between $h(k(+))1(+))R_m^{(k)}$ and the pieces of bidding rice information written on the bulletin board 25.

10 Step S5: If no match is found, decrement the price index k by one to $k \leftarrow k-1$ and return to step S3.

Step S6: For the index k for which the mach was found, write and publish all the random numbers $R_m^{(t)}$ ($k \leq t \leq K$) on the bulletin board 25.

15 Step S7: Determine k at this time as the winning price index, then output this index k and the identifier ID_m of the bidding device 10_m having submitted the winning bid, and discontinue the current bid-opening session.

When the lowest bidding price bid is chosen as the successful bid in this case, the index k is set to the smallest possible value, 1 in this example, in step S2 in Fig. 19, then in step S4 the index k is incremented by one, and in step S5 all random numbers $R_m^{(t)}$ which are $1 \leq t \leq k$ are published on the bulletin board 25. The other operations are the same as those described above with reference to Fig. 19.

25 While in the above the select information $b_m^{(k)}$ has been described to be "0" or "1," they may be any values as long as they are two predetermined different integers.

SIXTH EMBODIMENT

In the second embodiment described previously, at the time of bidding each bidding device 10_m sends the bidding price information $\gamma_m = g(h^{km}(IV_m))$ and the verification information $C_m = h^{k+1}(IV_m)$ to the bid-opening device 20, and at the time of bid-opening the bid-opening device 20 requests the bidding device 10_m to send the information $D_m = h^k(IV_m)$, and verifies whether $h(D_m)$ and C_m match for the information D_m received from the bidding device 10_m ; if they match, then the bid-opening device 20 further verifies whether $g(D_m)$ matches the bidding price information γ_m . These verifications need to be made for all of $m = 1, 2, \dots, M$. Accordingly, the amount of data to be processed increases with an increase in the number M of bidding devices used. In addition, the larger the highest value K of the index k , the more the amount of multiple processing by the one-way function h ; hence it is necessary to process an enormous amount of data.

To avoid this, the sixth embodiment utilizes one-way functions to transform the bidding price index k_m to $gm = H_m^{(K)} = h^{K-km}(g^{xm}(IV_m))$, which is sent to the bid-opening device 20. x_m is an arbitrary integer equal to or greater than 1 which is determined by the bidding device 10_m . When inquired about whether it has bid with the index k , the bidding device 10_m presents $H_m^{(k-1)} = h^{k-km-1}(g^{xm}(IV_m))$ if k is not its aimed bidding price index k_m , and if it is the aimed value, the bidding device 10_m presents $H_m^{(k-1)} = g^{xm-1}(IV_m)$. The bid-opening device 20 verifies the former with $h(H_m^{(k-1)}) = H_m^{(K)}$ and the latter with $g(H_m^{(k-1)}) = H_m^{(K)}$.

The M bidding devices 10_m indirectly bit the bidding price index values k_m to the bid-opening device 20, which detects the largest one of the index values k_m bit by the bidding devices 10_m . Each bidding device 10_m and the bid-opening device 20 have a conversion table in which K bidding prices

PR_1, PR_2, \dots, PR_K are held in a one-to-one correspondence with K kinds of index values $1, 2, \dots, K$ in increasing order. In this embodiment, as the index value k (where $k = 1, 2, \dots, K$) increases, the value PR_k becomes larger; for example, $PR_1 = 10, PR_2 = 15, PR_3 = 30, \dots, PR_K = 3000$.

5 Fig. 20 illustrates in block form the functional configuration of the bidding device 10_m and Fig. 21 is a flowchart showing its bidding procedure. The bidding device 10_m comprises an input part 11, a control part 13, a bidding price transformer 14, a transceiver 18 and a storage part 12 all of which are interconnected via a common bus 10B. The bidding price
10 transformer 14 is made up of a conversion table 15, a one-way function h processor 16 and a one-way function g processor 17. The control part 13 reads out a bidding procedure program stored in the storage part 12, and follows it to control the respective parts to perform bidding as described below.

15 Step S1: The bidding device 10_m receives via the input part 11 a value PR_m selected from values PR_1, PR_2, \dots, PR_K , an initial value (a positive integer) IV_m and an arbitrary integer x_m equal to or greater than 1.

Step S2: The control part 13 stores IV_m and x_m in the storage part 12.

20 Step S3: The control part 13 refers to the conversion table 15 with PR_m to convert it to an index value k_m and stores it in the storage part 12.

Step S4: The initial value IV_m and the bidding price x_m are read out from the storage part 12, then input to the one-way function g processor 17, wherein the initial value is processed x_m times with the one-way function g to obtain $g^{x_m}(IV_m)$.

25 Step S5: If necessary, $g^{x_m}(IV_m)$ is stored in the storage part 12.

Step S6: $g^{x_m}(IV_m)$, K and k_m are input to the one-way function h processor 16, wherein $g^{x_m}(IV_m)$ is processed $K - k_m$ times with the one-way

function h to obtain

$$H_m^{(K)} = h^{K-k_m}(g^{x_m}(IV_m)).$$

Step S7: $H_m^{(K)}$ is sent as the bidding price information to the bid-opening device 20 via the transceiver 18.

5 In this way, the bidding device 10_m sends the aimed bidding price index value k_m to the bid-opening device 20.

Step S8: Upon beginning the bid-opening procedure by the bid-opening device 20 after the bidding, each bidding device 10_m receives an inquiry with the price index k from the bid-opening device 20 by the transceiver 18 as depicted in Fig. 21.

Step S9: A check is made to see if the inquiry index value k is equal to the bidding price index k_m stored in the storage part 12.

Step S10: If not equal, $g^{x_m}(IV_m)$ is read out of the information storage part 12 and is input to the one-way function h processor 16 together with k_m and k , wherein $g^{x_m}(IV_m)$ is processed $k-k_m-1$ times with the one-way function h to obtain response information $H_m^{(k-1)}$ by the following equation:

$$H_m^{(k-1)} = h^{k-k_m-1}(g^{x_m}(IV_m))$$

Step S11: The bidding device 10_m sends the response information $H_m^{(k-1)}$ to the bid-opening device 20 via the transceiver 18 and waits for the next inquiry about k .

Step S12: If the inquiry about k corresponds to its aimed value, that is, if the index k is equal to k_m in the storage part 12, the bidding device 10_m inputs the initial value IV_m and x_{m-1} to the one-way function g processor 17, wherein the initial value IV_m is processed x_m-1 times to obtain response information $H_m^{(k-1)} = g^{x_m-1}(IV_m)$.

Step S13: The bidding device 10_m sends the response information $H_m^{(k-1)}$ to the bid-opening device 20.

The functional configuration of the bid-opening device 20 is depicted in Fig. 22 and its bid-opening procedure in Fig. 23. The bid-opening device 20 comprises a control part 21, a program storage part 27S, a one-way function h processor 22, a one-way function g processor 23, a counter 24, a bulletin board 25, a conversion table 25A, a transceiver 28, and an information storage part 25, all of which are interconnected via a common bus 20B.

Step S1: Upon receiving the bidding information $\gamma_m = H_m^{(K)}$ from each bidding device 10_m by the transceiver 28, the control part 21 writes the bidding information $H_m^{(K)}$ on the bulletin board 25 to publish it.

Step S2: Set K as the initial value of k in the counter 24.

Step S3: Send the index value k on the counter 24 to each bidding device 10_m , and send thereto an inquiry about bidding via the transceiver 28.

Step S4: Receive the response information $H_m^{(k-1)}$ by the transceiver 28 from all the bidding devices 10_m .

Step S5: Input $H_m^{(k-1)}$ to the one-way function h processor 22 to process it with the one-way function h to obtain $h(H_m^{(k-1)})$.

Step S6: Check whether the result of operation $h(H_m^{(k-1)})$ is equal to the bidding information A_m for m in the storage part 35.

Step S7: If $h(H_m^{(k-1)}) = H_m^{(K)}$, store the received information $H_m^{(k-1)}$ as updated bidding information $H_m^{(K)}$ in the storage part 35 to update $H_m^{(K)}$.

Step S8: Decrement the count value k of the counter 24 by one, then return to step S3, and inquire of each bidding device 10_m about whether it has made a registration for the value k.

Step S9: When it is found in step S6 that the response information $H_m^{(k-1)}$ from the bidding device 10_m is $g^{xm-1}(IV_m)$ which is equal to the aimed index value, $h(H_m^{(k-1)})$ does not become equal to $H_m^{(K)} = h^{ek+1-km-1}(g^{xm}(IV_m)) =$

$g^{xm}(IV_m)$ in step S9. Then, input $H_m^{(k-1)}$ to the one-way function g processor 23 to process $H_m^{(k-1)}$ with the one-way function g to obtain $g(H_m^{(k-1)})$.

Step S10: Make a check to see if $g(H_m^{(k-1)})$ is equal to $H_m^{(K)}$ corresponding to m stored in the storage part 35.

5 Step S11: When the bidding device 10_m has performed correct processing, $h^{km+1-km-1}(g^{xm}(IV_m)) = g^{xm}(IV_m) = H_m^{(K)}$ by the process of step S7 at the time of previous inquiry for $k = k_{m+1}$; hence, $g(H_m^{(k-1)}) = H_m^{(K)}$ holds. In the inquiry processing for the index k which is decremented one by one, the index k for which $g(H_m^{(k-1)}) = H_m^{(K)}$ holds for the first time is the maximum
10 value among the bidding price indexes of all the bidding devices, and this index k is converted to the value PR_k by referring to the conversion table 25A.

Step S12: Output the value PR_k as the highest one of the bid values, and if necessary, output the number m of the winning bidding device 10_m as well.

15 In the bidding procedure of Fig. 21, if $k = k_m$ in step S9 when inquired about whether it has bid k , the bidding device 10_m may send to the bid-opening device 29 in step S13 not only the response information $H_m^{(k-1)}$ but also information indicating $k = k_m$ (which information will hereinafter be referred to as identity information). In this instance, upon receiving the
20 response information $H_m^{(k-1)}$ in step S4 in Fig. 23, the bid-opening device 20 makes a check for the identity information; if not having received it, the device 20 performs the operation $h(H_m^{(k-1)})$ and if having received the information, $g(H_m^{(k-1)})$. Incidentally, in the event that $g(H_m^{(k-1)}) \neq H_m^{(K)}$ in step S10 in Fig. 23, the bid-opening device 20 may discontinue the current
25 bid-opening session for the reasons of dishonesty by the bidding device concerned and request all the bidding devices 10_m to rebid; alternatively, the bid-opening device 20 may abandon inquiring that bidding device but may

continue inquiring the other bidding device.

In the case where the bidding prices PR_k are arranged on each of the conversion tables 15 and 25A in such a decreasing order as 3000, 2950, 2900, ..., 100 in correspondence with the K index values 1, 2, ..., K , the price PR_k corresponding to the index value k for which $g(H_m^{(k-1)}) = H_m^{(K)}$ holds for the first time in the inquiry about bidding k represents the lowest one of the aimed bidding prices of all the bidding devices 10_m . The maximum value of the index may also be obtained without using the conversion table 15. In this instance, the bidding device 10_m sends the index value k_m , and after step S10 in Fig. 23 the bid-opening device 20 outputs the index value k as the highest value and, if necessary, together with the number m (or ID_m) of the bidding device 10_m having sent the index value k_m .

In the bid-opening procedure depicted in Fig. 23, the bid-opening device 20 inquires every bidding device 10_m for each value of the index $k = K, K-1, K-2, \dots$, and receives $H_m^{(k-1)}$, and then processes it using the one-say function h in step S5; hence this procedure requires high communication cost and computational complexity. In Fig. 24 there is depicted a modified form of the above-mentioned bid-opening procedure whose communication cost and computational complexity are reduced using the scheme described previously with reference to Fig. 11. No description will be given of the bidding procedure since it is exactly the same as in the Fig. 11 embodiment.

Step S0: Receive bidding price information $H_m^{(K)} = h^{K-k_m}(g^{x_m}(IV_m))$ and the identifier ID_m from each bidding device.

Step S1: Publish the received $H_m^{(K)}$ and ID_m on the bulletin board 25.

Step S2: Set the initial value of the index k at K .

Step S3: Inquire of all the bidding devices 10_m about whether they bid for the index k .

Step S4: Check the responses for YES (which means that the bidding device concerned has bid for the index k).

Step S5: If no YES is found, decrement k by one and returns to step S3 to repeat the same processing.

5 Step S6: If YES is found, request all the bidding devices 10_m to send their bidding price information $H_m^{(k-1)}$. The response of the bidding device to this request is the same as described previously in connection with Fig. 21.

Step S7: Publish the received information $H_m^{(k-1)}$ on the bulletin board
25.

10 Step S8: For the response $H_m^{(k-1)}$ of an m (representing the bidding device 10_m) having bid for the index k, compute

$$H_m = h^{K-k}(g(H_m^{(k-1)}))$$

and for the responses $H_m^{(k-1)}$ from the other m's (the other bidding devices), compute

15 $H_m = h^{K+1-k}(H_m^{(k-1)}).$

Step S9: Check whether $H_m = H_m^{(k)}$ holds for all the m's, and if a mismatch is detected for even one of them, send an error message to all the bidding devices and discontinue the current bid-opening session.

20 Step S10: If a match is detected for every one of them, determine that the bidding device 10_m of the number m having responded YES is the winning bidder, and output the index k at that time and its identifier ID_m for publication

The bidding device 10_m and the bid-opening device 20 can each be implemented by a computer:

25

SEVENTH EMBODIMENT

In the fifth embodiment described previously, each bidding device 10_m

generates the select information $b_m^{(k)}$ indicating whether to bid for every price index $k = 1, 2, \dots, K$, and these pieces of select information are contained in K pieces of information $h(k(+))b_b^{(k)}(+))R_m^{(k)}$, where $k = 1, 2, \dots, K$. In this embodiment, however, the plural pieces of select information are contained in a single piece of bidding price information through multiple processing with the one-way function h .

Fig. 25 illustrates in block form the functional configuration of each bidding device 10_m . Assume that K bidding prices PR and the k price indexes $k = 1, 2, \dots, K$, which have a one-to-one correspondence with each other, are both arranged in monotone increasing order in the same direction. The bidding select information for each index k will be identified as $b^{(k)}$. In this embodiment a select information generating part 54 does not generate the select information $b_m^{(k)}$ for all the indexes $k = 1, 2, \dots, K$ but instead generates the select information $b_m^{(k)}$ only for indexes higher than the bidding price index k_m . $H_m^{(k)} = h(H_m^{(k-1)} || b_m^{(k)})$ is calculated, with $H_m^{(k_m-1)} = IV_m$ as its initial value, for each value of the price index $k (=k_m, k_m+1, \dots, K)$ by a one-way function h processor 16, a concatenator 55 and a buffer 56, and the calculation result $H_m^{(k)}$ for each value of k is stored in a data storage part 14S. The final calculation result $H_m^{(K)}$ will hereinafter be called bidding price information. In this embodiment, a signature $Sig_m(H_m^{(K)})$ is generated by a signature generator 14S for the bidding price information 57.

Fig. 26 is a flowchart showing the bidding procedure of the bidding device 10_m depicted in Fig. 25.

In this embodiment, letting k_m be the index that the bidding device 10_m bids, a select information generating part 54 generates $K-k_m+1$ pieces of select information $b_m^{(k_m)}, b_m^{(k_m+1)}, \dots, b_b^{(K)}$ corresponding to the indexes larger than the bidding price index k_m (step S1). Then, $H_m^{(k_m-1)}, H_m^{(k_m)}, H_m^{(k_m+1)}, \dots,$

$H_m^{(K)}$ are successively generated by the following equations

$$H_m^{(km-1)} = IV_m$$

$$H_m^{(km)} = h(H_m^{(km-1)} || b_m^{(km)})$$

$$H_m^{(km+1)} = h(H_m^{(km)} || b_m^{(km+1)})$$

5 :

$$H_m^{(t)} = h(H_m^{(t-1)} || b_m^{(t)})$$

:

$$H_m^{(K)} = h(H_m^{(K-1)} || b_m^{(K)})$$

and they are stored in the data storage part 14S (step S2). Further, a
 10 signature $\sigma_m = \text{Sig}_m(H_m^{(K)})$ of the bidding device 10_m corresponding to the
 bidding price information $H_m^{(K)}$ is generated by the signature generator 14S
 (step S3). The bidding device 10_m sends $H_m^{(K)}$, σ_m and ID_m as bidding
 information to the bid-opening device 20 (step S4). After this, the bid-
 opening procedure is started, and upon receiving an inquiry for each value of
 15 the index k , the bidding device reads out $\{H_m^{(k-1)}, b_m^{(k)}\}$ from the data storage
 part 14S, and sends it to the bid-opening device (step S5).

The bid-opening device 2- comprises, as depicted in Fig. 27, a control
 part 21, a one-way function h processor 22, a counter 24, a bulletin board 25,
 an information storage part 35, comparators 58 and 59 and a signature verifier
 20 33. The pieces of bidding information $H_m^{(K)}$, σ_m and ID_m are written on the
 bulletin board 25. Then, the received information $H_m^{(k-1)}$ is processed by the
 one-way function h processor 22 to obtain $H_m^{(k)} = h(H_m^{(k-1)})$, which is
 compared by the comparator 58 with $H_m^{(k)}$ read out of the bulletin board 25 to
 thereby verify whether they match. Further, it is checked by the comparator
 25 59 whether the received select information $b_m^{(k)}$ is 1, and if it is 1, then the
 bidding device 10_m corresponding to m at that time is determined as the
 winning bidder.

Fig. 28 is flowchart showing the bid-opening procedure of the bid-opening device 20.

The bid-opening device 20 verifies respective signatures σ_m (where $m = 1, 2, \dots, M$) and writes and publish the received pieces of information $H_m^{(K)}$, σ_m and ID_m on the bulletin board 25.

The bid-opening device 20 sends k to the bidding device in the order $[k = K, K-1, K-2, \dots]$ and asks for information $\{H_m^{(k-1)}, b_m^{(k)}\}$ corresponding to each index k . The information $\{H_m^{(k-1)}, b_m^{(k)}\}$ received from each bidding device 10_m is published on the bulletin board 25, then it is checked whether $H_m^{(k)} = h(H_m^{(k-1)}, b_m^{(k)})$ holds for the information $H_m^{(k)}$ received previously, and if it holds, it is checked whether the select information $b_m^{(k)}$ is 1. When $b_m^{(k)}$ is 0 for all of $m = 1, 2, \dots, M$, the bid-opening device 20 decrements k to $k \leftarrow k-1$, then sends again k to the bidding device and asks for the information $\{H_m^{(k-1)}, b_m^{(k)}\}$, thereafter performing the same operation as described above.

If the select information $b_m^{(k)}$ is 1 for any one of $m = 1, 2, \dots, M$, then the bidding device 10_m corresponding to that m is determined as the winning bidder. The bid-opening device 20 publishes the successful bidding price index k_m and the identifier ID_m of the wining bidding device 10_m on the bulletin board 25.

According to this embodiment, since each bidding device does not perform the multiple processing with the one-way function for indexes smaller than the bidding price index k_m , the computational complexity is low accordingly.

The bid-opening device performs the bid-opening procedure as described below.

Step S0: Receive the pieces of bidding information $H_m^{(K)}$, σ_m and ID_m from each bidding device, then verifies respective signature σ_m (where $m = 1,$

2, ..., M), and writes and publishes the pieces of information $H_m^{(K)}$, σ_m and ID_m on the bulletin board 25.

Step S1: Set the initial value of the index k to K .

Step S2: Send k to each bidding device 10_m and ask for $\{H_m^{(k-1)}, b_m^{(k)}\}$.

5 Step S3: Write and publish on the bulletin board 25 the information $\{H_m^{(k-1)}, b_m^{(k)}\}$ received from each bidding device 10_m .

Step S4: Process the received information $\{H_m^{(k-1)}, b_m^{(k)}\}$ by the one-way function h processor 22, thereby generating $H = h(H_m^{(k-1)} || b_m^{(k)})$.

10 Step S5: Verify by the comparator 58 whether H generated in step S4 matches the previously received $H_m^{(k)}$. If a mismatch is detected, then send an error message to the bidding device and discontinue the current bid-opening session.

Step S6: If no mismatch is found in step S5, then decides that the response from every bidding device is valid, and make a check by the
15 comparator 59 to see if the received select information $b_m^{(k)}$ is 1.

Step S7: When the select information $b_m^{(k)}$ from all bidding devices 10_m is 0, update k with $k-1$ and return to step S2.

Step S8: When any one of M pieces of select information $b_m^{(k)}$ is 1 in step S6, determine that the bidding device 10_m corresponding to m , which
20 provides that information $b_m^{(k)}$, is the winning bidder, and write and publish its identifier ID_m and the index k_k of the winning bid on the bulletin board 25, and end the bid-opening procedure.

In this embodiment the prices bid by the unsuccessful bidders are each kept secret from the other participants. The lowest price bid can be made a
25 successful bid by using a conversion table wherein the price PR monotonously increases in the direction opposite to that in which the index k monotonously increases.

Incidentally, it is also possible to set $H_m^{(0)} = IV_m$, $H_m^{(1)} = h(H_m^{(0)} || b_m^{(1)})$, ..., $H_m^{(K)} = h(H_m^{(K-1)} || b_m^{(K)})$, where $b_m^{(1)} = b_m^{(2)} = \dots = b_m^{(km-1)} = 0$.

The communication cost and computational complexity involved in the bid-opening procedure of Fig. 27 can also be reduced, as depicted in Fig. 27', by the application of the scheme described previously with reference to Fig. 11. The bidding procedure is exactly the same as in Fig. 25, and hence it will not be described.

Step S0: Receive the bidding price information $H_m^{(K)} = h(\dots h(h(H_m^{(km-1)} || b_m^{(km)})) || b_m^{(km+1)}) \dots || b_m^{(K)})$ and the identifier ID_m from each bidding device.

10 Step S1: Publish the received $H_m^{(K)}$ and ID_m .

Sep S2: Set the initial value of the index k at K .

Step S3: Inquire of all the bidding devices 10_m about whether they bid for the index k .

15 Step S4: Check the responses for YES (which means that the bidding device concerned has bid for the index k).

Step S5: If no YES is found, decrement k by one and returns to step S3 to repeat the same processing.

Step S6: If YES is found, request all the bidding devices 10_m to send their bidding price information $H_m^{(k-1)} = h(\dots h(h(H_m^{(km-1)} || b_m^{(km)})) || b_m^{(km+1)}) \dots || b_m^{(K)})$. The response of the bidding device to this request is the same as described previously in connection with Fig. 21. For the bidding device having bid for the current index k , $k = k_m$; therefore, $H_m^{(k-1)} = H_m^{(km-1)} = IV_m$.

25 Step S7: Publish the received information $H_m^{(k-1)}$ on the bulletin board.

25 Step S8: For the response $H_m^{(k-1)}$ of an m (representing the bidding device 10_m) having bid for the index k , compute

$$H_m = h(\dots h(h(H_m^{(k-1)} || 1) || 0) || \dots 0)$$

and for the responses $H_m^{(k-1)}$ from the other m 's (the other bidding devices), compute

$$H_m = h(\dots h(h(H_m^{(k-1)}) \parallel 0) \parallel 0) \dots \parallel 0).$$

Step S9: Check whether $H_m = H_m^{(k)}$ holds for all the m 's, and if a mismatch is detected for even one of them, send an error message to all the bidding devices and discontinue the current bid-opening session.

Step S10: If a match is detected for every one of them, determine that the bidding device 10_m of the number m having responded YES is the winning bidder, and output the index k at that time and its identifier ID_m for publication.

EIGHTH EMBODIMENT

In each of the embodiments described above, the bidding prices for the bidding price indexes $k = 1, 2, \dots, K$ in the conversion table are discrete values such as 1000, 2000, 3000, ..., 10000, and each bidding device bids any one of the K prices but cannot bid a value intermediate between such discrete prices unless K prices are set in "1" increments. This embodiment is intended to permit bidding an arbitrary price intermediate between the discrete values. In this embodiment, an arbitrary bidding price PR within the range defined by the highest and lowest bidding prices is expressed by the following equation.

$$PR = F(k) + Q$$

$$\text{where: } 0 \leq Q < F(k+1) - F(k)$$

$F(k)$ represents the price corresponding to the index k specified on the conversion table, and Q will hereinafter be referred to as a fraction.

This embodiment is one that the bidding price PR defined above is applied to the first embodiment described previously. Bidding price

information $g(h^k(IV_m))$ and Q_m are sent to the bid-opening device 20. Further, $h^{k+1}(IV_m)$ is sent as verification information to the bid-opening device 20 together with the bidding price information. These pieces of information are published on the bulletin board as is the case with the first embodiment.

Fig. 30 is a block diagram illustrating the configuration of each bidding device 10_m , which is identical with the bidding device of the first embodiment except that the bidding price transformer 14 is provided with a fraction calculating part 14a. The fraction calculating part 14A calculates, for a desired bidding price PR_m , $Q_m = PR_m - F(k_m)$ from the index k_m read out of the conversion table 15. As is the case with the first embodiment, the one-way function h processor 16 and the one-way function g processor 17 are used to compute $\gamma_m = g(h^{k_m}(IV_m))$ from the index k_m which satisfies $F(k_m+1) > PR_m \geq F(k_m)$ and the initial value IV_m . In this embodiment, γ_m , Q_m and ID_m are sent as bidding information to the bid-opening device 20.

The bid-opening device 20 has, as depicted in Fig. 31, a sequencer 61 added to the bid-opening device 20 in Fig. 6 embodiment. The pieces of bidding information γ_m , Q_m and ID_m are written and published on the bulletin board 25. The sequencer 61 reads out Q_1, Q_2, \dots, Q_M from the bulletin board 25, then sequences them in descending order, and sequences $m = 1, 2, \dots, M$ corresponding to the sequenced Q_m , thereafter outputting them in the sequential order. The control part 21 checks, for each index k , whether ID_m and γ_m match each other in the sequence of m defined by the sequencer 61. The bidding device 10_m , which corresponds to m for which the match was detected for the first time, is determined as the winning bidder.

Fig. 32 is a flowchart depicting the bid-opening procedure of the bid-opening device 20 shown in Fig. 31, which steps S0 to S7 are identical with steps S0 to S7 in Fig. 7 but differ in step 8 and the subsequent steps.

Roughly speaking, steps S8 and S9 are new steps added between steps S7 and S8 in Fig. 7. Step S8 and the subsequent steps will be described below.

In step S8 the bid-opening device 20 makes a check to determine whether the matching in steps S6 to S11 has been completed for all fractions Q_m for the current value of k . If not completed, the procedure goes to step S9. In step S9, the bid-opening device 20 selects the largest one of the remaining fractions Q_m to determine the corresponding m . In step S10, the device 20 reads out of the data storage part 36 updated data $D_m^{(k)} = h^k(IV_m)$ corresponding to that m , and processes the read-out data by the one-way function g processor 23, thereby updating it such that $D_m^{(k)} \leftarrow g(D_m^{(k)})$. In step S11, the control device 21 makes a check to see if the updated data $D_m^{(k)}$ corresponding to m matches the bidding price information γ_m corresponding to m on the bulletin board 25, and if not, then the procedure returns to step S8.

When it is decided in step S8 that the matching for all the fractions Q_m for the current k has been completed, the bid-opening device 20 decrements k by one in step S12, and returns to step S8, repeating the same procedure as mentioned above. When it is decided in step S11 that the updated data $D_m^{(k)}$ and the bidding price information γ_m match, the bid-opening device 20 determines in step S13 that the index k at that time is the successful index, and outputs the identifier ID_m corresponding to that information γ_m and the successful bidding price $F(k) + Q_m$ (or merely the index k).

Since $D_m^{(k)}$ and γ_m are matched for the current value of the index k in the descending order of the fractions Q_m as described above, the highest bidding price can be determined at the first detection of matching between $D_m^{(k)}$ and γ_m . The value m selected in step S9 is determined by the sequencer 61 which sequences in descending order the fractions Q_1, Q_2, \dots, Q_M read out of the bulletin board 25, and sequences m correspondingly, as explained

before.

In the case where the lowest bidding price bid is a successful bid, the bidding prices are arranged in monotonous increasing order in the direction opposite to that in which the values of the index k are arranged in monotonous decreasing order, and the sequencer 61 sequences the fractions Q_1, Q_2, \dots, Q_M in ascending order, and sequences m correspondingly. In step S9 the smallest one of the unprocessed fractions Q_m is chosen, and the corresponding m is determined. The sequencer 61 determines the order of m .

The technique that uses many fractions Q_m as described above can be applied not only to the first embodiment but also to the other embodiments explained heretofore.

Electronic Competitive Auction System With Provisional Identifier Device

In the embodiments described above, since the bidding device identifier ID_m is contained in the bidding information and sent to the bid-opening device 20, it can be said that these embodiments employ what is called a sealed-bit auction system. Fig. 33 illustrates in block form an electronic competitive auction system which uses a provisional identifier registration device to implement a secret-bit auction.

Each bidding device 10_m is adapted to communicate with a provisional identifier registration device 70. Referring to Fig. 34, the operation of this electronic competitive auction system will be described below.

Step S0: Notice of auction is input to each bidding device 10_m .

Step S1: Upon receiving the notice of auction, the bidding device 10_i outputs the identifier ID_m to the provisional identifier registration device 70.

Step S2: For the identifier ID_m provided thereto, the provisional identifier registration device 70 issues a provisional identifier AID_m , then

stores ID_m and AID_m in pair form on a recording medium 71, and sends the provisional identifier AID_m to the bidding device 10_i.

Step S3: The bidding device 10_m: generates the bidding price PR_m ;

Step S4: Transforms the bidding price PR_m to the bidding price information γ_m ; and

Step S5: Sends the bidding price information γ_m and the provisional identifier AID_m to the bid-opening device 20.

Step S6: The bid-opening device 20: calculates a successful bid from the bidding price indexes received from all the bidding devices; and

Step S7: Outputs the successful bid and the provisional identifier of the bidding device having offered the successful bid.

Thus, it is possible to keep the auction participants secret. Incidentally, when inquiring the provisional identifier registration device 70, the bid-opening device 20 can learn the identifier ID_m corresponding to the successful bid from the provisional identifier AID_m . This method can be applied to all of the embodiments explained hereinbefore.

The bidding device 10_m and the bid-opening device 20 can be implemented by interpreting and executing programs with a computer.

20 EFFECT OF THE INVENTION

As described above, according to the present invention, since the bidding price is transformed to a bidding price information through utilization of a one-way function and is then sent to the bid-opening device, it is possible to keep the bidding price of each bidding device secret from the other bidding devices prior to bidding, ensuring fairness of auction.

By publishing $h^{K+1}(IV_m)$ and $h^{kmx}(IV_m)$ corresponding to a winning bidding price on the bulletin board, it is possible for all bidding devices to

verify whether the winning bidding price was correctly bid without being altered.

Furthermore, the present invention permits determination of the winning bid while hiding the other bidding prices.

5 According to the second embodiment, the bids of losing bidders, except the winning bid, are kept secret even from the bid-opening device.

According to the third embodiment, the bids of losing bidders, except the winning bid, are kept secret even from the bid-opening device, and in addition, the amount of data for communication with the bidding device can
10 be reduced.

According to the fourth embodiment, there is no fear of the bidding price of each bidding device being revealed to the other devices, and at the bid-opening time the successful bid can easily be specified directly from the bidding price; furthermore, the validity of the winning bid can be verified.

15 According to the fifth embodiment, bidding price information including each bidding price index is generated using a one-way function, and the bidding price information for all bidding price indexes is sent to the bid-opening device; hence, the aimed bidding price can be kept secret.

20 According to the sixth embodiment, either $h(H_m^{(k-1)}) = H_m^{(K)}$ or $g(H_m^{(k-1)}) = H_m^{(K)}$ needs only to be verified for each index value and for each bidding device.

25 According to the seventh embodiment, each bidding device generates the bidding price information including select information for only indexes larger than the bidding price index k_m in the fifth embodiment, the computational complexity can be reduced.

According to the eighth embodiment, since a desired bidding price is expressed by the sum of fractions Q of a price $F(k)$ corresponding to the index

k, an arbitrary price can be bid with a small number of indexes.

000120-00000000